

$$40 \quad |2 - x^2 + x| = 2$$

$$\left[\frac{1 \pm \sqrt{17}}{2}; 0; 1 \right]$$

$$\textcircled{1} \begin{cases} 2 - x^2 + x \geq 0 \\ \cancel{2 - x^2 + x = 2} \end{cases} \vee \textcircled{2} \begin{cases} 2 - x^2 + x < 0 \\ -(2 - x^2 + x) = 2 \end{cases}$$

$$\textcircled{1} \begin{cases} x^2 - x - 2 \leq 0 \\ x^2 - x = 0 \end{cases} \quad \begin{matrix} x_1 = -1 \quad x_2 = 2 \\ (x-2)(x+1) \leq 0 \\ x(x-1) = 0 \end{matrix} \quad \begin{cases} -1 \leq x \leq 2 \\ x=0 \vee x=1 \end{cases}$$

$$x=0 \vee x=1$$

$$\textcircled{2} \begin{cases} x^2 - x - 2 > 0 \\ x^2 - x - 4 = 0 \end{cases} \quad \begin{cases} x < -1 \vee x > 2 \\ x = \frac{1 \pm \sqrt{17}}{2} \end{cases} \quad x = \frac{1 \pm \sqrt{17}}{2}$$

$$\Delta = 1 + 16 = 17$$

$$x=0 \vee x=1 \vee x = \frac{1 \pm \sqrt{17}}{2}$$

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$$\left| x + \frac{1}{2}(x-1) - \frac{x}{3} \right| = \frac{2}{3}$$

$$\left[-\frac{1}{7}; 1 \right]$$

$$\left| \frac{6x + 3(x-1) - 2x}{6} \right| = \frac{2}{3}$$

$$\left| \frac{6x + 3x - 3 - 2x}{6} \right| = \frac{2}{3}$$

$$\left| \frac{7x - 3}{6} \right| = \frac{2}{3}$$

$$\frac{|7x - 3|}{6} = \frac{2}{3}$$

$$\cancel{6} \cdot \frac{|7x - 3|}{\cancel{6}} = \frac{2}{\cancel{3}} \cdot \cancel{6}^2$$

$$|7x - 3| = 4$$

$$\begin{cases} 7x - 3 \geq 0 \\ 7x - 3 = 4 \end{cases} \vee \begin{cases} 7x - 3 < 0 \\ -7x + 3 = 4 \end{cases}$$

$$\begin{cases} x \geq \frac{3}{7} \\ x = 1 \end{cases} \vee \begin{cases} x < \frac{3}{7} \\ x = -\frac{1}{7} \end{cases}$$

$$\boxed{x = 1 \quad \vee \quad x = -\frac{1}{7}}$$

METODO DI RISOLUZIONE ALTERNATIVO (EQUIVALENTE)

$$|f(x)| = g(x)$$

$$\begin{cases} g(x) \geq 0 \\ f(x) = \pm g(x) \end{cases} \Rightarrow \begin{cases} g(x) \geq 0 \\ f(x) = g(x) \end{cases} \vee \begin{cases} g(x) \geq 0 \\ f(x) = -g(x) \end{cases}$$

66 $|x^2 - 2| = x$

[1; 2]

METODO NUOVO

$$\begin{cases} x \geq 0 \\ x^2 - 2 = \pm x \end{cases} \Rightarrow \begin{cases} \textcircled{1} \\ x \geq 0 \\ x^2 - 2 = x \end{cases} \vee \begin{cases} \textcircled{2} \\ x \geq 0 \\ x^2 - 2 = -x \end{cases}$$

$$\begin{aligned} \textcircled{1} \begin{cases} x \geq 0 \\ x^2 - x - 2 = 0 \end{cases} & \begin{cases} x \geq 0 \\ (x-2)(x+1) = 0 \end{cases} & \begin{cases} x \geq 0 \\ x = 2 \vee x = -1 \end{cases} \\ & & \text{N.ACC.} \\ & & x = 2 \end{aligned}$$

$$\begin{aligned} \textcircled{2} \begin{cases} x \geq 0 \\ x^2 + x - 2 = 0 \end{cases} & \begin{cases} x \geq 0 \\ (x+2)(x-1) = 0 \end{cases} & \begin{cases} x \geq 0 \\ x = -2 \vee x = 1 \end{cases} \\ & & \text{N.ACC.} \\ & & x = 1 \end{aligned}$$

$x = 1 \vee x = 2$

METODO VECCHIO

$$|x^2 - 2| = x$$

$$\textcircled{1} \begin{cases} x^2 - 2 \geq 0 \\ x^2 - 2 = x \end{cases} \quad \vee \quad \textcircled{2} \begin{cases} x^2 - 2 < 0 \\ -x^2 + 2 = x \end{cases}$$

$$\textcircled{1} \begin{cases} x \leq -\sqrt{2} \vee x \geq \sqrt{2} \\ x^2 - x - 2 = 0 \end{cases} \quad \begin{cases} x \leq -\sqrt{2} \vee x \geq \sqrt{2} \\ (x-2)(x+1) = 0 \end{cases} \quad \begin{cases} x \leq -\sqrt{2} \vee x \geq \sqrt{2} \\ \text{N.A.C.} \\ x = 2 \vee x = -1 \end{cases}$$

$$x = 2$$

$$\textcircled{2} \begin{cases} -\sqrt{2} < x < \sqrt{2} \\ -x^2 - x + 2 = 0 \end{cases} \quad \begin{cases} -\sqrt{2} < x < \sqrt{2} \\ x^2 + x - 2 = 0 \end{cases} \quad \begin{cases} -\sqrt{2} < x < \sqrt{2} \\ (x+2)(x-1) = 0 \end{cases}$$

$$\begin{cases} -\sqrt{2} < x < \sqrt{2} \\ \text{N.A.C.} \\ x = -2 \vee x = 1 \end{cases}$$

$$x = 1$$

$$\boxed{x = 1 \vee x = 2}$$

ESEMPI

$$a) |x-3| = 2$$

$$\begin{cases} 2 \geq 0 & \leftarrow \text{VERA } \forall x \\ x-3 = \pm 2 \end{cases} \quad \begin{cases} x \in \mathbb{R} \\ x-3 = \pm 2 \end{cases} \Rightarrow$$

$$x-3 = 2 \quad \vee \quad x-3 = -2$$

$$\boxed{x = 5 \quad \vee \quad x = 1}$$

$2 \geq 0$ È VERA PER OGNI $x \in \mathbb{R}$

⇓

$2 + 0 \cdot x \geq 0$ perché la immagine
costante

$$b) |x-3| = -2$$

$$\begin{cases} -2 \geq 0 & \leftarrow \text{FALSA } \forall x \\ \dots \end{cases} \quad \begin{cases} \emptyset \\ \dots \end{cases}$$

IMPOSSIBILE

75 $|x^3 - 4x| = x + 2$

$[-2; 1; 1 \pm \sqrt{2}]$

MEZODO VECCHIO

$$\begin{cases} x^3 - 4x \geq 0 \\ x^3 - 4x = x + 2 \end{cases} \vee \begin{cases} x^3 - 4x < 0 \\ -x^3 + 4x = x + 2 \end{cases}$$

MEZODO NUOVO

$$\textcircled{1} \begin{cases} x + 2 \geq 0 \\ x^3 - 4x = x + 2 \end{cases} \vee \textcircled{2} \begin{cases} x + 2 \geq 0 \\ x^3 - 4x = -(x + 2) \end{cases}$$

$$\textcircled{1} \begin{cases} x \geq -2 \\ x^3 - 5x - 2 = 0 \end{cases}$$

DIVISORI DI -2 : $\pm 1, \pm 2$

$+2 \mapsto 8 - 10 - 2 \neq 0$

$-2 \mapsto -8 + 10 - 2 = 0$ OK!

$$\begin{array}{ccc|c} 1 & 0 & -5 & -2 \\ -2 & & & \\ \hline 1 & -2 & -1 & // \end{array}$$

$(x^2 - 2x - 1)(x + 2) = 0$ $x^2 - 2x - 1 = 0$ $\frac{\Delta}{4} = 1 + 1 = 2$

$$\begin{cases} x = -2 \vee x = 1 \pm \sqrt{2} \\ x \geq -2 \end{cases} \text{ tutte e tre accettabili}$$

$X = -2 \vee X = 1 \pm \sqrt{2}$

$$\textcircled{2} \begin{cases} x+2 \geq 0 \\ x^3 - 4x = -(x+2) \end{cases}$$

$$\begin{cases} x \geq -2 \\ x^3 - 3x + 2 = 0 \end{cases}$$

$$\begin{array}{ccc|c} & 1 & 0 & -3 & 2 \\ 1 & & 1 & 1 & -2 \\ \hline & 1 & 1 & -2 & // \end{array}$$

$$\begin{cases} x \geq -2 \\ (x^2 + x - 2)(x - 1) = 0 \end{cases}$$

$$\begin{cases} x \geq -2 \\ (x+2)(x-1)(x-1) = 0 \end{cases}$$

$$\begin{cases} x \geq -2 \\ (x+2)(x-1)^2 = 0 \end{cases}$$

$$\begin{cases} x \geq -2 \\ x = -2 \vee x = 1 \\ \text{entrambe accettabili} \end{cases}$$

$$x = -2 \vee x = 1$$

Soluzioni finali $\textcircled{1} \vee \textcircled{2}$

$$x = -2 \vee x = 1 \pm \sqrt{2} \vee x = 1$$