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$$x^2 - (2 + 2i)x + 2i - 1 = 0$$

[i, 2 + i]

$$\Delta = (2 + 2i)^2 - 4(2i - 1) = \cancel{4} - \cancel{4} + \cancel{8i} - \cancel{8i} + 4 = 4$$

$$x = \frac{2 + 2i \pm 2}{2} = \begin{cases} \frac{2i}{2} = i \\ \frac{2 + 2i + 2}{2} = \frac{4 + 2i}{2} = 2 + i \end{cases}$$

$$x = i \vee x = 2 + i$$

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$$x^3 - 8i = 0$$

[i ± √3, -2i]

$$x^3 = 8i$$

Calcolo le 3 radici cubiche di $8i = 8\left(\cos\frac{\pi}{2} + i\sin\frac{\pi}{2}\right)$

$$z_0 = \sqrt[3]{8} \left(\cos\frac{\pi}{6} + i\sin\frac{\pi}{6}\right) = 2\left(\frac{\sqrt{3}}{2} + i\cdot\frac{1}{2}\right) = \sqrt{3} + i$$

$$\begin{aligned} z_1 &= \sqrt[3]{8} \left(\cos\left(\frac{\pi}{6} + \frac{2}{3}\pi\right) + i\sin\left(\frac{\pi}{6} + \frac{2}{3}\pi\right)\right) = \\ &= 2\left(\cos\frac{5}{6}\pi + i\sin\frac{5}{6}\pi\right) = 2\left(-\frac{\sqrt{3}}{2} + i\cdot\frac{1}{2}\right) = -\sqrt{3} + i \end{aligned}$$

$$\begin{aligned} z_2 &= \sqrt[3]{8} \left(\cos\left(\frac{\pi}{6} + \frac{4}{3}\pi\right) + i\sin\left(\frac{\pi}{6} + \frac{4}{3}\pi\right)\right) = \\ &= 2\left(\cos\frac{3}{2}\pi + i\sin\frac{3}{2}\pi\right) = 2(0 + i\cdot(-1)) = -2i \end{aligned}$$

$$x = \pm\sqrt{3} + i \vee x = -2i$$